



Heat is dissipated by radiation & convection

(a) Radiation

$$\begin{aligned} \dot{Q}_{\text{rad}} &= \epsilon \sigma A (T_s^4 - T_a^4) \\ &= 0.92 \times 5.67 \times 10^{-8} \times 0.8 \times 1 \left( (273+70)^4 - (273+21)^4 \right) \\ &= 266 \text{ Watts / side} \\ &= \underline{532 \text{ W/m}} \end{aligned}$$

(b) Convection

$$Gr = \frac{\beta g \rho^2 l^3 \Delta T}{\mu^2}$$

with  $\beta = \frac{1}{T}$   $Gr = \frac{g \rho^2 l^3 \Delta T}{T \mu^2}$

At  $40^\circ\text{C}$   $\rho = \frac{273}{273+40} \times \frac{1}{0.773} = 1.128 \text{ kg/m}^3$   $\beta = \frac{1}{273+40}$

$\mu = 0.019 \times 10^{-3} \text{ kg/sm}$   $\lambda = 0.0272 \text{ W/mK}$

$$\therefore Gr = \frac{9.81 \times 1.128^2 \times 0.8^3 (70-21)}{(273+40) (0.019 \times 10^{-3})^2} = \underline{2771 \times 10^6}$$

$$\therefore Nu = 0.378 (2771 \times 10^6)^{0.25} = 86.7$$

$$h = \frac{\lambda Nu}{L} = \frac{0.0272 \times 86.7}{0.8} = 2.95 \text{ W/m}^2\text{K}$$

$$\dot{Q}_{\text{conv.}} = h A \Delta T = 2.95 \times 0.8 \times 1 \times 2 (70-21) = \underline{231 \text{ W/m}}$$

Total  $\dot{Q}/m = 532 + 231 = 763 \text{ W/m}$

$\therefore$  Length for 1000 W =  $\frac{1000}{763} = \underline{1.31 \text{ m}}$