

## Data sheet

Unless told otherwise in a question, you may assume the following:

Density of water =  $1000 \text{ kgm}^{-3}$

Atmospheric pressure =  $101.3 \text{ kPa}$

Acceleration due to gravity =  $9.81 \text{ ms}^{-2}$

The universal gas constant,  $R_0 = 8314. \text{ J kmol}^{-1} \text{ K}^{-1}$

## Formulae list

All the symbols have their usual meanings.

### Reaction turbines and pumps:

$$u_r = \frac{\dot{V}}{2\pi r B}$$

$$u_w = \frac{u_r}{\tan \alpha}$$

$$\tan \beta = \frac{u_r}{u_w - U}$$

where  $U$  is the tangential speed of the impeller

$$T = \dot{m}(u_{w1}r_1 - u_{w2}r_2)$$

### For an ideal gas:

$$c_p - c_v = R$$

### For a reversible adiabatic process:

$$p_1 V_1^\gamma = p_2 V_2^\gamma \quad \text{also} \quad \frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{\gamma-1} = \left(\frac{p_2}{p_1}\right)^{(\gamma-1)/\gamma}$$

$$W = \frac{p_2 V_2 - p_1 V_1}{\gamma - 1} = m c_v (T_2 - T_1)$$

### For a reversible constant pressure process:

$$W = p(V_1 - V_2) = mR(T_1 - T_2) \quad Q = m c_p (T_2 - T_1)$$

### For a reversible constant temperature (isothermal) process:

$$W = mRT \ln\left(\frac{V_1}{V_2}\right) = p_1 V_1 \ln\left(\frac{V_1}{V_2}\right) \quad Q = -W$$

**For a reversible constant volume process:**

$$W = 0$$

$$Q = mc_v(T_2 - T_1)$$

**For a reversible polytropic process:**

$$p_1 V_1^n = p_2 V_2^n$$

$n$  is the polytropic index

$$\frac{T_2}{T_1} = \left(\frac{V_1}{V_2}\right)^{n-1} = \left(\frac{p_2}{p_1}\right)^{(n-1)/n}$$

$$W = \frac{p_2 V_2 - p_1 V_1}{n-1}$$

$$Q = mc_v(T_2 - T_1) - W$$